







Research Program of the Boyd Research Group

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The visuals of this talk will be posted at boydnlo.ca/presentations or elsewhere

Presented at the Annual Meeting of the Max Planck - University of Ottawa Centre for Extreme and Quantum Electronics, October 30, 2019.

Schedule of Presentation

Robert Boyd (5 min): Intro to the group research program

Jeremy Upham (12 min):

NLO of epsilon-near-zero (ENZ) materials: Large nonlinear index change in ITO, time refraction, holography, ENZ nonlinearity of a multi-layer stack.

Orad Reshef (12 min):

Large nonlinearity in antenna-coupled ITO, surface lattice resonance (SLR) in metasurfaces, SLR in ITO, four-wave mixing in zero-index waveguides.

Boris Braverman (12 min):

AOMs for rapid modulation of quantum states , bright squeezed vaccum

Research Themes

- Nonlinear Optics
- Nano Optics
- Quantum Optics

Our Research Group





STUDIES OF ENZ MATERIALS

Adiabatic wavelength conversion (also known as "time refraction") in ITO Nonlinear properties of layered composite metal-dielectric ENZ materials OAM generation from circular epsilon-near-zero (ENZ) waveguide structures Pump-probe spectroscopy of u-shaped antennas on ITO for active polarization metasurfaces Superradiance studies

PLASMONICS

Metasurfaces for spectral filtering

LIGHT DRAG EXPERIMENTS

Transverse photon drag in ruby

Transverse photon drag in rubidium vapour using EIT

QUANTUM OPTICS

Entanglement generation with an incoherent pump Three photon entanglement via three-photon downconversion Induced coherence without induced emission (in both spontaneous and high-gain limits) Looking for high-order correlations in high-gain PDC Quantum imaging: Phase imaging with high-gain PDC

NONLINEAR OPTICS

Nonlinear interactions in a rubidium nanocell Nonlinearity in GRIN fiber and mode self-cleaning Nonlinear microscopy of biological samples and graphene-like carbon Fast mode generation/analysis with AOM (two experiments)

Epsilon-near-zero and zero-index materials

Orad Reshef, Boyd Research Group

Department of Physics University of Ottawa, Canada

Max Planck Centre Annual Meeting October 30, 2019



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Zero-index metamaterials







Zero-index metamaterials





By adding nanostructured antennas to an ITO surface, we can further enhance ENZ-based nonlinearities.



M. Z. Alam et al, Nat. Photonics 12, 79 (2018)







Mohammad Karimi PhD Student



1 NLO in structured ITO

















All-optical beam-steering





Active optical surfaces using ENZ-enhanced nonlinear optics Experiments are underway:







High quality-factor metasurfaces using Surface Lattice Resonances (SLRs) in plasmonic nanoparticle arrays





Saad Bin Alam PhD Student



1

Active optical surfaces using ENZ-enhanced nonlinear optics



Ryan Hogan PhD Student



SLR



Read our review article!

REVIEWS

Nonlinear optical effects in epsilon-near-zero media

Orad Reshef^{[b]*}, Israel De Leon^{[b2}, M. Zahirul Alam^[b] and Robert W. Boyd^{1,3*}

Abstract | Efficient nonlinear optical interactions are essential for many applications in modern photonics. However, they typically require intense laser sources and long interaction lengths, requirements that often render nonlinear optics incompatible with new nanophotonic architectures in integrated optics and metasurface devices. Obtaining materials with stronger nonlinear properties is a crucial step towards applications that require lower powers and smaller footprints. Recently, a new class of materials with a vanishing permittivity, known as epsilonnear-zero (ENZ) materials, has been reported to exhibit unprecedented ultrafast nonlinear efficiencies within sub-wavelength propagation lengths. In this Review, we survey the work that has been performed on ENZ materials and the related near-zero-index materials, focusing on the observation of various nonlinear phenomena (such as intensity-dependent refraction, four-wave mixing and harmonic generation), the identification of unique field-enhancement mechanisms and the study of non-equilibrium dynamics. Degenerately doped semiconductors (such as tin-doped indium oxide and aluminium-doped zinc oxide) are particularly promising candidates for ENZ-enhanced nonlinear optical applications. We conclude by pointing towards possible future research directions, such as the search for ENZ materials with low optical losses and the elucidation of the mechanisms underlying nonlinear enhancements.

NATURE REVIEWS | MATERIALS

VOLUME 4 | AUGUST 2019 | 535





Zero-index metamaterials







Zero-index metamaterials







We can engineer our own ENZ materials out of silicon using Dirac Cone metamaterials:



SOI PhC waveguide that supports a mode at the $\frac{2\pi n}{\lambda} = 0$ point of the brillouin zone



Reshef, O. et al. ACS Photonics 4, 2385–2389 (2017)





We can also engineer our own ENZ materials out of silicon using Dirac Cone metamaterials:

2



Rep. Prog. Phys. 82 (2019) 012001 (18pp)

https://doi.org/10.1088/1361-6633/aad3e5

Key Issues Review

Manipulating the flow of light using Dirac-cone zero-index metamaterials

Jin zone

Daryl I Vulis[®], Orad Reshef[®], Philip Camayd-Muñoz and Eric Mazur¹

Department of Physics and School of Engineering and Applied Sciences, Harvard University, 9 Oxford Street, Cambridge, MA 02138, United States of America



Reshef, O. et al. ACS Photonics 4, 2385-2389 (2017)



Zero-index metamaterials radiate light normal to their surfaces



$n\sin\theta = 0 \implies \theta = 0$

2

Reshef, O. et al. ACS Photonics 4, 2385–2389 (2017)



For a gap that is too large for traditional evanescent coupling, a zero-index waveguide can radiate light from one waveguide to another.



Codey Nacke



zero-index silicon waveguides





Zero-index-based couplers may couple light even for separations that exceed the free space wavelength $(\lambda = 1550 \text{ nm})$.

The effect is broadband, working for *low* index as well.









We can achieve critical coupling (>10 dB extinction ratio) over 50 nm bandwidth with an edge-to-edge gap of 2 μ m. Circumference = 250 µm -10 Transmission Ratio in dB -12 -22 -30 -22 -30 7 unit cells -35 2 µm -40 Zero-index ring resonator -45 Conventional ring resonator 1.52 1.54 1.56 1.58 1.6 1.62 1.64 1.66 1.7 1 68 Wavelength [µm]

FSR: 3 nm, as expected Transmission loss: 20 dB, due to large propagation losses

1



Experiments are underway:







Nonlinear properties of Zero-index waveguides:





Nonlinear properties of Zero-index waveguides:



2















forward and backward

















So we measured this in the lab!



Justin Gagnon MSc Student





So we measured this in the lab!





Justin Gagnon MSc Student









2




So we measured this in the lab!



2



Justin Gagnon MSc Student





Summary

The large nonlinearity of ITO can further be enhanced using nanostructured.

We are even capable of locally defining the nonlinear properties of a surface using nanostructures.

We can also make "ENZ" metamaterials using silicon. These devices also have interesting linear + nonlinear properties:

surface-normal radiation

"directionless" phase-matching



Thank you



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Research in Quantum Photonics

• Boyd Group, University of Ottawa

Boris Braverman, October 30, 2019



Outline

Correlations in high-gain PDC



Jeremy Rioux

Samuel Lemieux

Girish Kulkarni

Rapid generation and detection of spatial modes of light using AOMs



Alexander Skerjanc

Nicholas Sullivan Xialin

Liu





Samuel Lemieux Jeremy Rioux Girish Kulkarni

Correlations in High-Gain PDC



High-Gain Parametric Down-Conversion (PDC)

Imaging with squeezed light Two-mode bright squeezed vacuum state: $1 \sum_{n=1}^{\infty} c_{n}$

$$|TMSV\rangle = \frac{1}{\cosh G} \sum_{n=0}^{\infty} (-e^{i\phi} \tanh G)^n |n_s \otimes n_i\rangle$$

Below shot-noise correlations, quantified by the noise reduction factor (NRF):

$$NRF = \frac{\langle var(N_s - N_i) \rangle}{\langle N_s + N_i \rangle}$$





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signal

idler

crystal

pump

High-Gain PDC

Imaging with squeezed light



Goal: Implement phase imaging with:

- Supersensitivity (NRF<1)
- Superresolution $(\lambda_{eff} = \lambda_p)$





Correlations in High-Gain PDC

TMSV: NRF should be independent of G

- Larger *G* should give more signal! Experimental observation: NRF usually increases near-linearly with *G*
- Technical imperfections or intrinsic effect? How can we benefit from using higher *G* for quantum-enhanced sensing?
- Better alignment?
- Structuring the pump beam?
- Using higher-order correlations?



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Quantum State of High-Gain PDC



What is the full state coming out of the high-gain PDC process?

- Quadratic interaction Hamiltonian: $H = \int dk_i dk_s c_{i,s} (\alpha_p a_s^{\dagger} a_i^{\dagger} + H.C.)$
- No loss or decoherence → output is a pure, Gaussian state
- Bloch-Messiah decomposition can be used to represent state
- How many modes need to be mixed together in the mode basis change?
 - TMSV: only 2

 $|\Psi\rangle = U_{mode \ basis \ change} U_{diag,sq} |0\rangle$



• How strong are the higher-order correlations? How can they be controlled/used?



Assume perfect phase matching for collinear modes $(q_s = q_i = 0)$

Derive Bogolyubov transformation for output modes in terms of input modes: $a_s(q_j, L) =$ $= \sum_i c_{i,j} a_s(q_i, 0) + d_{i,j} a_i^{\dagger}(q_i, 0)$

Calculate expectation values for photon numbers, correlations



High-Gain PDC Model – Single-mode properties

Photon number grows as $\langle n_s \rangle \propto \sinh^2(E_p)$ Angular spectrum of phase matching broadens with gain



High-Gain PDC Model – Signal-Idler Correlations

Correlation width grows with gain "Speckle shape" is maximally non-Gaussian at $G \approx 1.5$





High-Gain PDC Model – NRF







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High-Gain PDC Model – Next Steps

Observing below-SQL correlations at large *G* requires increasingly precise alignment

• What is the largest SNR attainable with a realistic experiment?

Look for higher-order correlations

- Bogolyubov \rightarrow Bloch-Messiah
- Consider simplified model with fewer modes

Extend model to 2 spatial dimensions









Alexander Skerjanc Nicholas Sullivan Xialin Liu

Rapid Generation and Detection of Spatial Modes of Light Using AOMs



Acousto-Optic Modulators (AOMs)

Sound waves induce density variations, which diffract the light

- Acts as a rapidly steerable mirror High-dimensional free-space QKD
- Require fast generation of different modes of light
- Speed limited by SLM refresh rates Use an AOM to select one of a set of fixed holograms



Rapid Generation of Modes

Switch between one of five sections of SLM1, each encoding a different OAM mode Analyze state with SLM2 Refresh rates up to 500 kHz











19

20

21



23

24

22

Real-Time Quantum State Tomography

D Η +1 A

-1

Mode generation ~ mode projection

- Hilbert space spanned by OAM +1, -1
- Need to perform one of 6 measurements

Each setting is measured for 100 µs

Overall measurement bandwidth is $\approx 1 \, \text{kHz}$





AOM as a Spatial Light Modulator

What if the sound wave is not just a single frequency?

- Can generate multiple values of *q* simultaneously!
- Because pattern is dynamic (frequency shift), need to use a pulsed laser

Potential applications to shaping modes of very intense lasers that would damage SLMs, i.e. for structured-beam high-gain PDC

• Spatial analogue to an acousto-optic programmable dispersive filter







Double-slit interference





Quantum Photonics Research Themes

PDC in unconventional parameter regimes and systems:

- Very strong (high gain) pumping
- Very weak (single-photon) pumping
- Effect of incoherent pumping on entanglement

Applications to quantum metrology

- Absolute photon number measurement
- Superresolution and supersensitivity
- Trans-color measurement

Control of light propagation

- Mode sorting in waveguides
- AOMs for mode control
- Slow light in moving media

Applications to adaptive optics

- Nonlocal aberration cancelation with entangled photons
- Mode cleaning in nonlinear fibers
- Digital phase conjugation with vector beams





Light drag effects in slow-light media



10

8

6

4

0 0 0

1,050

950

n₂ (m² W⁻¹

Real-time holography with ENZ nonlinearity



 θ increases

1,450

1,250 1,350



Time refraction in ENZ





1,150

Wavelength (nm)





Correlations in high-gain PDC



Spatial mode control with AOMs





Appendix

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High-Gain PDC

Primary Radiation Standard based on Quantum Nonlinear Optics

 Calibration of photon number, based on simple and fundamental properties of PDC

Photon number \mathcal{N} depends on:

Gain function \mathcal{G}

- Pump amplitude \mathcal{E}_p
- Crystal length *L* Vacuum amplitude *Q* Phase matching function *S*



Vacuum amplitude





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S. Lemieux, E. Giese, R. Fickler, M.V. Chekhova, R.W. Boyd, Nat. Phys., 15, 529 (2019)



High-Gain PDC

Primary Radiation Standard based on Quantum Nonlinear Optics



Relative calibration at **low gain**: single photon pairs with well-known spectral shape





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S. Lemieux, E. Giese, R. Fickler, M.V. Chekhova, R.W. Boyd, Nat. Phys., 15, 529 (2019)

Absolute

calibration at

high gain:

exponential

increase in



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Induced Coherence Without Induced Emission

Previous experiments: CW laser pump, observe single photons

- Imaging with undetected photons
- Transcolor sensing

Extensions:

- Coherence *with* induced emission: strongpumping regime
- Highly non-degenerate regime: THz spectroscopy
- Guaranteeing absence of induced emission: single-photon pump





Free-Space Mode Sorting Using Waveguides

Free-space communication with "interesting" basis states: OAM, LG, HG, ...

- propagation invariant, high information density
 Problem: how to efficiently generate and detect?
- State of the art with free-space optics: q-plates and SLMs Eigenmodes of rectangular waveguides \approx HG modes
- Use integrated optics techniques to manipulate on-chip





Single-

mode

waveguide

Multi-mode

waveguide



Transmitter

PDM

2 modes

WDM B modes SDM

M modes Signal/Noise log₂(1+SNR)

Free-Space Mode Sorting Using Waveguides

Strategy:

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- Remove higher-order modes one by one
- Taper multimode waveguide to match sequential modes to a series of single-mode waveguides









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Free-Space Mode Sorting Using Waveguides

Result: 76.3% average sorting efficiency, 1.4% average cross-talk



TE₁₀ TE₁₁ TE₀₁ TE₀₁ 3 1 2 4



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Output mode

wa



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wa

Arbitrary Mode Transformations

- Modes are de-multiplexed into single-mode waveguides with our device
- On-chip interferometer arrays enable arbitrary operations with fast update rates
 - Thermal tuning: 100's of MHz
 - Electro-optic tuning: 10's of GHz
- Modes are multiplexed with a second mode sorter



Carolan et al., Science, 349, 711 (2015)



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Entangled Photons

Correlations can exist (often simultaneously) in any degree of freedom:

- Polarization (spin)
- Time & energy (spectral)
- Position & momentum (spatial)

If generated by SPDC with laser pump, produce a pure state

Perfect correlations!





Dispersion Cancellation

Start out with perfectly correlated photons (EPR state):

 $t_s = t_i, \qquad \omega_s = \omega_p - \omega_i$

 Frequency dispersion in signal photon lengthens its pulse and weakens time correlations

Perfect correlations can be recovered!

- Proposal for nonlocal scheme: Franson, PRA 45 3126 (1992)
- Experimental realization: MacLean *et al.* PRL **120** 053601 (2018)





Birefringence Cancellation

Polarization entanglement (spin singlet): $|\psi\rangle = \frac{|H_s V_i\rangle - |V_s H_i\rangle}{\sqrt{2}}$ Perturb signal photon, i.e. $|H_s\rangle \rightarrow |R_s\rangle$, $|V_s\rangle \rightarrow |L_s\rangle$: $|\psi'\rangle = \frac{|R_s V_i\rangle - |L_s H_i\rangle}{\sqrt{2}}$ Original state can be recovered:

- Locally: $|R_s\rangle \rightarrow |H_s\rangle$
- Non-locally: $|H_i\rangle \rightarrow |R_i\rangle$
- Both are a change of measurement basis





Aberration Cancellation

Conceptually, the same as dispersion cancellation: $t \rightarrow X$. $\omega \rightarrow P$

In practice, more challenging to align, but...

- Can select functional form & variable for aberration
 - Frequency dispersion fixed by material parameters
 - 2nd order frequency dispersion (GVD) typically dominates
 - Hard to implement temporal dispersion (a fast chirp!)
- Can be applied to imaging
 - Rather than spectroscopy/photon timing experiments





Aberration Cancellation

Initial entangled state:

$$\psi(p_s, p_i) = A(p_s - p_i) \times \nu(p_s + p_i) \times e^{i(\phi_s(p_s) + \phi_i(p_i))}$$

- Phase matching: $A(p_s p_i) = A_0 \operatorname{sinc}\left(\frac{l_c|p_-|^2}{4k_0}\right) \times \exp\left(-i\frac{l_c|p_-|^2}{4k_0}\right)$
- Pump angular spectrum: $v(p_s + p_i) = \exp\left(-\frac{|p_+|^2w^2}{4}\right)$
- Aberration (and compensation): $e^{i(\phi_s(p_s)+\phi_i(p_i))}$ Plane wave pump:

$$\nu(p_s + p_i) = \delta(p_s + p_i) \rightarrow p_s = -p_i$$

To recover the initial state, simply require

$$\phi_s(p) = -\phi_i(-p)$$








Experimental Results: 2nd Order



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Experimental Results: 2nd+3rd Orders



Momentum correlations (not shown) are unaffected, as expected Higher-order aberrations produce interesting, non-Gaussian two-photon wavefunctions

Impact of Pump Beam Profile

Perfect aberration cancelation can only be observed when the pump is a plane wave $\Delta \mathrm{p}_+^2 = 7(1) \ \mathrm{h}^2/\mathrm{mm}^2$ Two-photon 20momentum Aberration (h/mm)wavefunction: Theory Cancellation $2\Delta p$ <u>й</u>-20 $\begin{array}{l} \Delta(p_s + p_i) \\ \geq \Delta(p_p) \end{array}$ -40 -20 20 $\mathbf{0}$ mm p_s

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Position correlations:

 $\Delta x_{-}^2 = 0.0069(4) \text{ mm}^2$

Application: Ghost Imaging

Can correct for signal noise by acting on idler photon No need for adaptive optics at signal wavelength or near bucket detector Where does entanglement come in?

- Can compensate for aberrations in any plane (even a 3D distribution)
- "image" vs "hologram"



Quantum Optics with LEDs

Can entanglement be observed if the pump is incoherent? (c)



- EPR correlations degrade linearly with mode number
- No entanglement above a certain point!
- Next step: Polarization entanglement

Theory: E. Giese, R. Fickler, W. Zhang, L. Chen, R.W. Boyd, Phys. Scr. 93 084001 (2018) bovdnlo.ca Experiment: W. Zhang, R. Fickler, E. Giese, L. Chen, R.W. Boyd, Opt. Express, 27, 20745 (2019)



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Mode Cleaning in Nonlinear Fibers

Can adaptive optics be implemented passively, using nonlinear optics?



Analogous to polariton condensation

Modes thermalize via nonlinearity

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Kasprzak *et al.*, Nature **443** 409 (2006) Wu *et al.*, Nat. Photon. 1749-4893 (2019)



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Longitudinal Photon Drag

Light propagating through a traveling medium is dragged along (Fizeau, 1851)

- For slow light $(n_a \gg n)$, drag proportional to the group velocity: $\Delta Z = \frac{2\nu Ln^2}{\lambda c} \left(\frac{1}{n} - \frac{1}{n^2} + \frac{n_g - n}{n^2} \right)$
- A manifestation of the Doppler effect in a highly dispersive medium



bovdnlo.ca A. Safari, I. De Leon, M. Mirhosseini, O. Magaña-Loaiza, R. W. Boyd, PRL 116, 013601 (2016)

300 E

250 E

150 100

50

_0.6

-0.4

-0.2

 $\Delta u \, (m/s)$ 200



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Transverse Photon Drag

For transverse motion, no Doppler effect present

•
$$\Delta x = \frac{vL}{c} \left(n_g - \frac{1}{n} \right)$$

Drag is a consequence of medium-induced delay in pulse propagation

- Most easily understood in frame co-moving with medium
- Small non-dispersive contribution from stellar aberration







Photon Drag with Negative Group Velocity

Expect upstream photon drag

• Photons move opposite to the medium!

Analogous to superluminal group pulse propagation

- Peak of output pulse exits medium before input peaks
- Possible in conditions of reverse saturable absorption Potential experimental platforms:
- Highly-doped ruby crystal
- EIT in rubidium vapour







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